

Marek Balcerzak, Institute of Mathematics, Łódź University of Technology,  
Łódź, Poland. email: marek.balcerzak@p.lodz.pl

## IDEAL CONVERGENT SUBSEQUENCES AND REARRANGEMENTS

These are results obtained together with Sz. Głąb, M. Popławski and A. Wachowicz. Let  $\mathcal{I}$  be an ideal on  $\mathbb{N}$  which is either analytic or coanalytic. Assume that  $(f_n)$  is a sequence of functions with the Baire property from a Polish space  $X$  into a Polish space  $Z$ , which is divergent on a comeager set. We investigate the Baire category of  $\mathcal{I}$ -convergent subsequences and rearrangements of  $(f_n)$ . Our result generalizes a theorem of Kallman. A similar theorem for subsequences is obtained if  $(X, \mu)$  is a  $\sigma$ -finite complete measure space and a sequence  $(f_n)$  of measurable functions from  $X$  to  $Z$  is  $\mathcal{I}$ -divergent  $\mu$ -almost everywhere. Then the set of subsequences of  $(f_n)$ ,  $\mathcal{I}$ -divergent  $\mu$ -almost everywhere, is of full product measure on  $\{0, 1\}^{\mathbb{N}}$ . Here we assume additionally that  $\mathcal{I}$  has property (G).

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