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## ON THE DISCRETE IDEAL CONVERGENCE OF SEQUENCES OF QUASI-CONTINUOUS FUNCTIONS

All results presented here were obtained jointly with Piotr Szuca.

The notion of discrete convergence of a sequence of real functions was introduced by Császár and Laczkovich [Studia Sci. Math. Hungar., **10**, no. 3 (1975), 463–472]. Z. Grande [Acta Math. Hungar., **92** (2001), 39–50] characterized discrete Baire classes generated by the family  $\mathcal{QC}$  of quasi-continuous real-valued functions defined on a metric Baire space. In our work we consider an ideal version of this theorem: for an ideal  $\mathcal{I}$  we describe the discrete  $\mathcal{I}$ -Baire system generated by the family  $\mathcal{QC}$ . This description can be different for different ideals  $\mathcal{I}$ , e.g. for the ideal FIN of all finite sets (the classical case) and for the ideal  $\mathcal{I}_d$  of asymptotic density zero sets (the statistical convergence). Our goal is to describe Borel ideals  $\mathcal{I}$  for which ideal and ordinary discrete Baire systems coincide. This work is a continuation of our previous investigations from [Fund. Math. **232** (2016), 269–280], where we consider analogous results for a pointwise  $\mathcal{I}$ -convergence. Recently A. Kwela and M. Staniszewski proved analogous results for quasi-normal  $\mathcal{I}$ -convergence.

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